

# Gate-induced superconductivity in atomically thin MoS<sub>2</sub> crystals

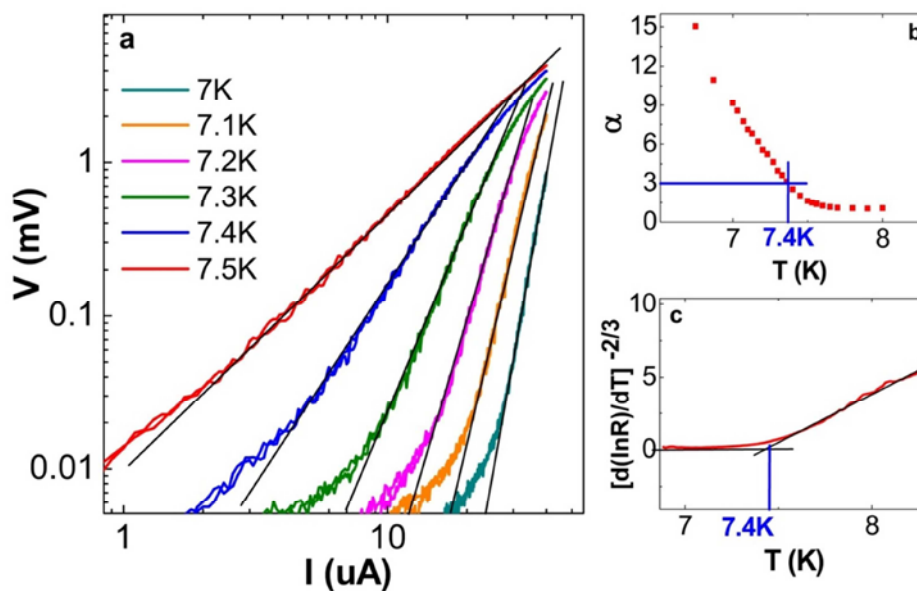
Davide Costanzo, Sanghyun Jo, Helmuth Berger, and Alberto F. Morpurgo

## Analysis of the $I$ - $V$ curves of superconducting 4L MoS<sub>2</sub> in terms of a Berezinskii-Kosterlitz-Thouless scenario.

The electrostatically induced superconducting state at the surface of an ionic-liquid gated MoS<sub>2</sub> transistor is expected to have a two-dimensional (2D) character, since the electrostatic screening length at a carrier density of  $10^{14}$  cm<sup>-2</sup> is approximately 1 nm<sup>1</sup>. According to the Mermin-Wagner theorem, in 2D systems, long-range order is suppressed by thermal fluctuations<sup>2</sup>; quasi-long-range ordering, however, can still occur. This quasi long-range ordering is characteristic of the Berezinskii-Kosterlitz-Thouless (BKT) mechanism for superconductivity, through which a coherent superconducting state occurs at a temperature  $T_{BKT}$ , lower than the mean-field critical temperature<sup>3 4</sup>.

There are different experimental manifestations of the BKT regime that can be looked for in the experiments, to see whether the observed behavior is compatible with that expected for 2D superconductivity. A well-known aspect of the BKT transition is the occurrence of power-law  $I$ - $V$  characteristics:  $V \propto I^\alpha$  where  $\alpha = 1$  for  $T$  well above  $T_{BKT}$ ,  $\alpha = 3$  for  $T = T_{BKT}$ , and  $\alpha > 3$  for  $T < T_{BKT}$ <sup>5 6</sup>. We have looked for such a behavior<sup>5 6</sup> in the  $I$ - $V$  curves measured in our devices. Fig. S1a shows the  $I$ - $V$  characteristic of a 4L MoS<sub>2</sub> FET (in log-log scale) measured below the onset temperature of superconductivity. A linear regime is clearly visible, whose slope  $\alpha$  (the exponent of the power law) increases upon lowering temperature, as expected. The exponent  $\alpha$  is obtained from fits of the slope for each temperature (black lines in Fig. S1a), and plotted as a function of temperature in Fig. S1b.  $\alpha$  increases with lowering  $T$  for temperatures well below the onset temperature, and  $\alpha = 3$  at  $T = 7.4$  K, providing a first estimate of  $T_{BKT}$ .

To confirm the BKT nature of the transition, we also looked at the temperature dependence of the resistance close to  $T_{BKT}$ . Theory predicts that  $R = R_0 \exp(-bt^{-1/2})$ , in contrast to the power law dependence expected in the Ginzburg-Landau theory ( $R_0$  and  $b$  are material dependent parameters, and  $t = T/T_{BKT} - 1$ )<sup>5,6</sup>. This functional dependence can be tested by checking that  $[d(\ln R)/dT]^{-2/3}$  varies linearly with  $T$  above  $T_{BKT}$ , and that it extrapolates at 0 for  $T = T_{BKT}$ . The data, shown in Fig. S1c, indeed displays the expected behavior. By extrapolating to zero the linear part of  $[d(\ln R)/dT]^{-2/3}$  we find that  $T_{BKT} = 7.4$  K, in good agreement with the previous estimation from the  $I$ - $V$  characteristic. The analysis of our experimental data is thus compatible with the theoretical expectation for a 2D BKT superconducting transition.



**Fig. S1. Berenzinskii-Kosterlitz-Thouless behavior in an ion-liquid gated 4L MoS<sub>2</sub> FET.**

**a.** Power-law dependence  $V \propto I^\alpha$  of the  $I$ - $V$  characteristics for different temperatures (below the onset of superconductivity) plotted in log-log scale. The solid black lines are best fits done to extract the exponent  $\alpha$ . **b.** Temperature dependence of  $\alpha$ .  $T_{BKT}$  corresponds to the value of  $T$  for which  $\alpha = 3$ , leading to  $T_{BKT} = 7.4$  K. **c.** Linear behavior of  $[d(\ln R)/dT]^{-2/3}$  as a function of temperature. The extrapolation to zero (black solid line) provides an independent estimate of  $T_{BKT}$ , which also gives 7.4 K, consistently with the analysis of  $I$ - $V$  characteristics.

## References

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